

Algebra 3-4 STUDY GUIDE FOR 1st Semester FINAL name _____ pd

- 1) Find the x- and y-intercepts for each function.

a) $y = -10x + 15$

X-int: Set $y=0$

$$0 = -10x + 15$$

$$-15 = -10x$$

$$\frac{-15}{-10} = x = 1.5$$

y-int: Set $x=0$

$$y = -10 \cdot (0) + 15$$

$$y = 15$$

b) $y = 8x^2 - 200$

X-int:

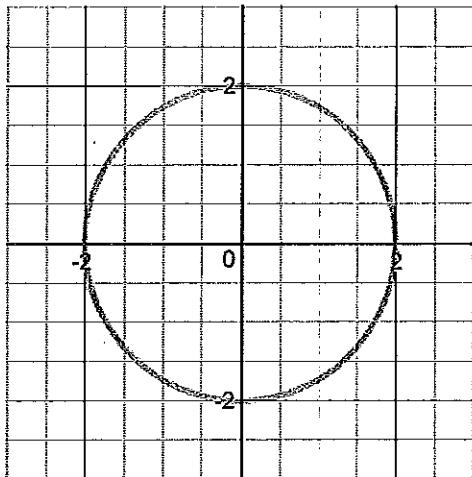
$$0 = 8x^2 - 200$$

$$200 = 8x^2$$

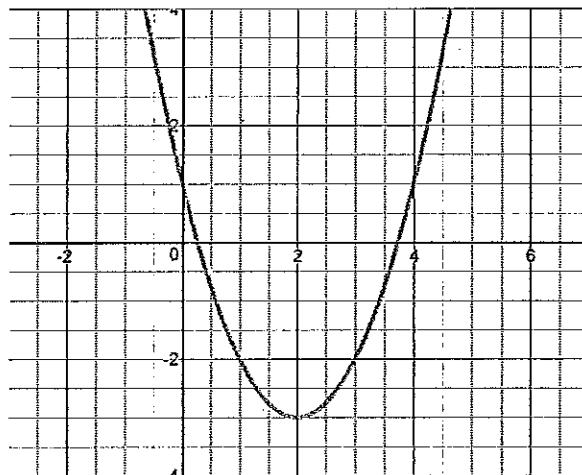
$$25 = x^2$$

$$\pm 5 = x$$

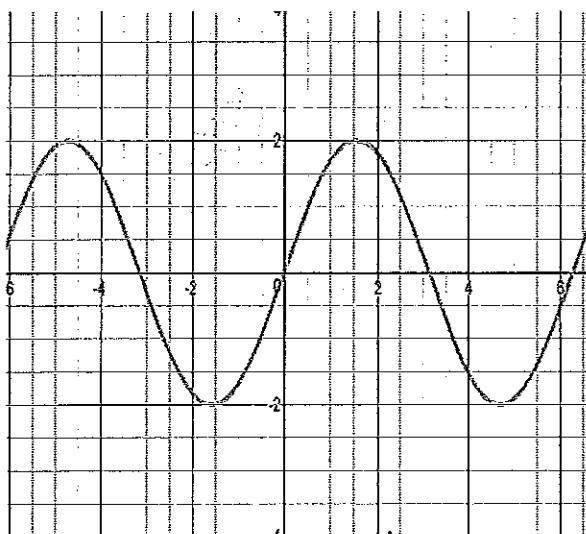
- 2) State the domain and range of each graph.



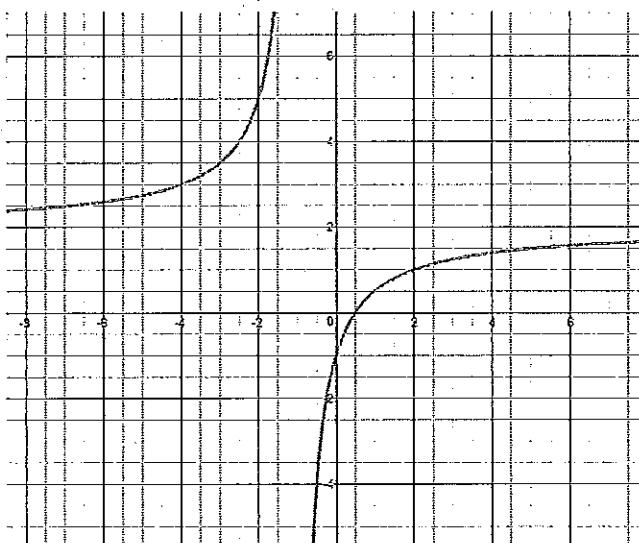
Domain: $[-5, 5]$
 Range: $[-5, 5]$



Domain: $(-\infty, \infty)$
 Range: $[-3, \infty)$



Domain: $(-\infty, \infty)$
 Range: $[-2, 6]$



Domain: $x \neq -1$ OR $(-\infty, -1) \cup (-1, \infty)$
 Range: $y \neq 2$ OR $(-\infty, 2) \cup (2, \infty)$

3) Graph the function.

State the x- and y-intercepts. $f(x) = 3\sqrt{x+3} - 4$

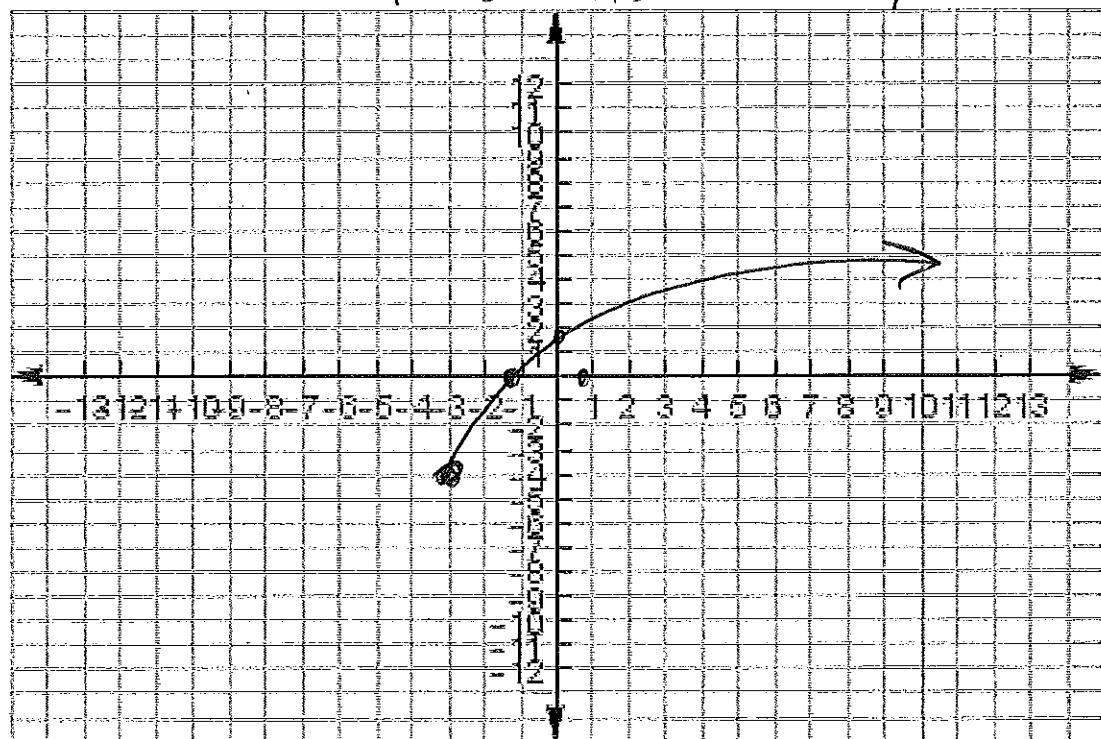
$$x\text{-int: } 0 = 3\sqrt{x+3} - 4$$

$$4 = 3\sqrt{x+3}$$

$$\frac{4}{3} = \sqrt{x+3}$$

$$\frac{16}{9} = x+3$$

$$\frac{16}{9} - 3x = 1.2$$



$$y\text{-int: } y = 3\sqrt{3} - 4$$

$$y \approx 1.196$$

4) Solve.

a) $4(8x - 1) + 3 = 7 - (x + 2)$

$$32x - 4 + 3 = 7 - x - 2$$

$$32x - 1 = 5 - x$$

$$33x = 6$$

$$x = \frac{6}{33}$$

b) $2(x + 3)^2 + 5 = 103$

$$2(x+3)^2 = 98$$

$$(x+3)^2 = 49$$

$$x+3 = \pm 7$$

$$x+3 = 7$$

$$x = 4$$

$$x+3 = -7$$

$$x = -10$$

c) $13 = 4\sqrt{x-5} - 1$

$$14 = 4\sqrt{x-5}$$

$$\frac{14}{4} = \sqrt{x-5}$$

$$\frac{7}{2} = \sqrt{x-5}$$

$$\frac{49}{4} = x-5, x = \frac{49}{4} + 5 = \frac{69}{4}$$

$$\cancel{3(4)^x = 192}$$

$$4^x = 64$$

$$\frac{4^1}{4^2} = \frac{4}{16}$$

$$4^3 = 64$$

$$x = 3$$

5) Given $f(x) = 3x^2 - 108$.

a) Find $f(0)$

$$\begin{aligned} 3(0)^2 - 108 \\ = -108 \end{aligned}$$

b) Solve for x if $f(x) = 0$

$$\begin{aligned} 3x^2 - 108 &= 0 \\ 3x^2 &= 108 \\ x^2 &= 36 \\ x &= \pm 6 \end{aligned}$$

6) Given $g(x) = \sqrt{x-1} + 3$.

a) Find $g(10)$

$$\begin{aligned} g(10) &= \sqrt{10-1} + 3 \\ &= \sqrt{9} + 3 \\ &= 3 + 3 = 6 \end{aligned}$$

b) Solve for x if $g(x) = 17$.

$$\begin{aligned} 17 &= \sqrt{x-1} + 3 \\ 14 &= \sqrt{x-1} \\ 196 &= x-1 \quad x = 197 \end{aligned}$$

7) Write the equation of the line that passes through the points $(-8, 1)$ and $(-24, -1)$.

$$m = \frac{-1-1}{-24-(-8)} = \frac{-2}{-16} = \frac{1}{8}$$

$$\begin{aligned} y &= \frac{1}{8}x + b \\ 1 &= \frac{1}{8}(-8) + b \end{aligned}$$

$$\boxed{y = \frac{1}{8}x + 2}$$

8) Simplify.

$$\begin{aligned} 1 &= -1+b \\ 2 &= b \end{aligned}$$

a) $\frac{a^{-3}b^4c^5}{a^6b^7}$

$$\frac{c^5}{a^9b^3}$$

b) $(3g^5h^0)^2$

$$9g^{10}$$

c) $\frac{(-4x^{-3}yw^5)^2}{(6xy^{-4}w)^3}$

$$\frac{16x^{-6}y^2w^{10}}{216x^3y^{-12}w^3}$$

$$\frac{2y^{14}w^7}{27x^9}$$

- 9) Investigate the function $f(x) = \frac{1}{2}x^3 + 2x - 6$

table:

X				
Y				

domain:

$$(-\infty, \infty)$$

range:

$$(-\infty, \infty)$$

x-intercept(s):

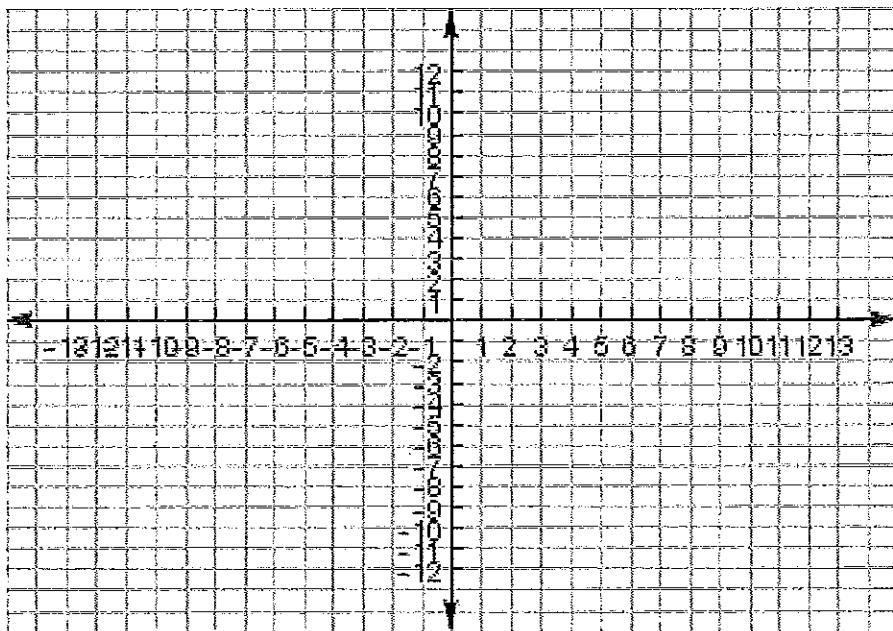
y-intercepts:

$$(0, -6)$$

asymptotes:

None

Graph:



- 10) Use the following sequence to answer a), b) and c): 6, 10, 14, ...

- a) Is the sequence arithmetic or geometric? Explain how you know.

Arithmetic \rightarrow adding 4.

- b) Give the explicit rule for the sequence.

$$f(x) = 6 + 4(x-1)$$

- c) Give the next three terms in the sequence.

18, 22, 26.

- 11) Use the following sequence to answer a), b) and c): 400, 200, 100, ...

- a) Is the sequence arithmetic or geometric? Explain how you know.

Geometric \rightarrow Multiply by $\frac{1}{2}$

- b) Give the explicit rule for the sequence.

$$f(x) = 400 \left(\frac{1}{2}\right)^{x-1}$$

- c) Give the next three terms in the sequence.

50, 25, 12.5

- 11) Write an arithmetic **and** a geometric rule for the given two terms. Then find the next three terms using each rule.

10, 15, ...

Arithmetic:

Add 5; $f(x) = 10 + 5(x-1)$; 20, 25, 30

Geometric:

Times 1.5; $f(x) = 10(1.5)^{x-1}$; 22.5, 33.75, 50.625

- 12) There are 30 deer living in a park. Their population doubles every month.

- a) Write an equation to represent their population after 'x' months.

$$y = 30(2)^x$$

- b) Is this an example of linear or exponential growth? Why?

Exponential, multiplying pattern.

- c) How many deer will there be in 10 months?

$$y = 30(2)^{10} = 30720$$

- 14) Suzi has \$3000 in an investment. It is depreciating at a rate of 9% per year.

- a) Write an equation for the situation. Define your variables.

$$y = \$, \quad x = \text{years}$$

$$y = 3000(0.91)^x$$

- b) Use your equation to find the value of the investment in ~~2017~~²⁰¹⁸.

$$y = 3000(0.91)^t$$

$$y = 2730$$

- c) When will the investment be worth less than \$1000?

$$y = \text{2nd-Table}, \quad \begin{array}{|c|c|} \hline x & y \\ \hline : & : \\ : & : \\ 10 & 1168.2 \\ 11 & 1063.1 \\ 12 & 967.43 \\ \hline \end{array}$$

- 15) Write an exponential equation of the curve that passes through (3, 17.28) and (7, 35.8318).

$$y = a \cdot b^x$$

$$17.28 = a \cdot b^3 \rightarrow a = \frac{17.28}{b^3}$$

$$35.8318 = a \cdot b^7$$

$$35.8318 = \frac{17.28}{b^3} \cdot b^7 \rightarrow \frac{35.8318}{17.28} = \frac{b^7}{b^3} \rightarrow 2.0735 = b^4$$

- 16) Find the vertex of the quadratic and write the equation in vertex form.
(use the method of finding 'h' from standard form and then finding 'k')

$$y = (x + 3)(x - 15)$$

$$x = -3, \quad x = 15$$

$$h = \frac{-3 + 15}{2} = \frac{12}{2} = 6$$

$$K = (6+3)(6-15)$$

$$(9)(-9)$$

$$-81$$

$$\text{Vertex: } (6, -81)$$

$$1.199 = b$$

$$1.22 b$$

$$a = \frac{17.28}{1.2^3}$$

$$a = 10$$

$$y = 10(1.2)^x$$

- 18) Multiply and simplify.

a) $(7x - 5)^2$

$$(7x - 5)(7x - 5)$$

$$49x^2 - 35x - 35x + 25$$

$$49x^2 - 70x + 25$$

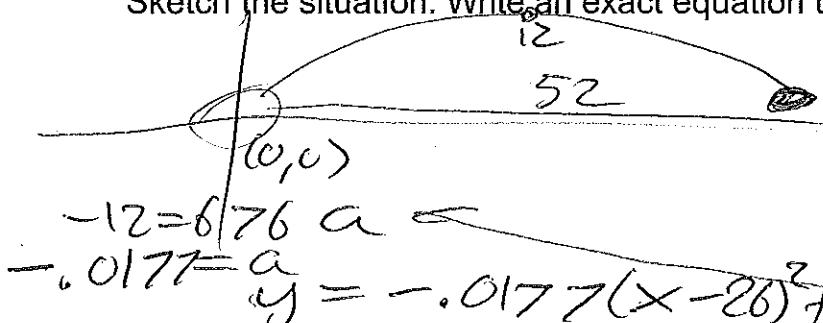
b) $8(x + 1)(4x - 9)$

$$8(4x^2 + 4x - 9x - 9)$$

$$8(4x^2 - 5x - 9)$$

$$32x^2 - 40x - 72$$

- 19) A ball is kicked from the ground and travels in a parabolic path. It travels a total horizontal distance of 52 feet and its maximum height reached is 12 feet. Sketch the situation. Write an exact equation to model the path of the ball.



$$\frac{52}{2} = 26 \text{ Vertex } = (26, 12)$$

$$y = a(x - 26)^2 + 12$$

$$0 = a(0 - 26)^2 + 12$$

$$-12 = a(26)^2$$

- 20) State which family each equation belongs to and the locator point of each.

$$y = \frac{1}{x-3}$$
 Linear $(3, 0)$

$$y = (x - 5)^2 - 7$$

$$\begin{matrix} \text{Quadratic} \\ \text{Parabola} \end{matrix} \quad (5, -7)$$

$$y = (x + 1)^3 \quad (-1, 0)$$

$$y = |x - 8| - 8$$
 Absolute value $(8, -8)$

$$y = \sqrt[3]{x} + 7$$
 Cube Root $(-7, 0)$

$$y = \sqrt{x - 2}$$
 Square root $(2, 0)$

- 21) Rewrite into vertex form by completing the square.

$$y = x^2 - 12x + 51$$

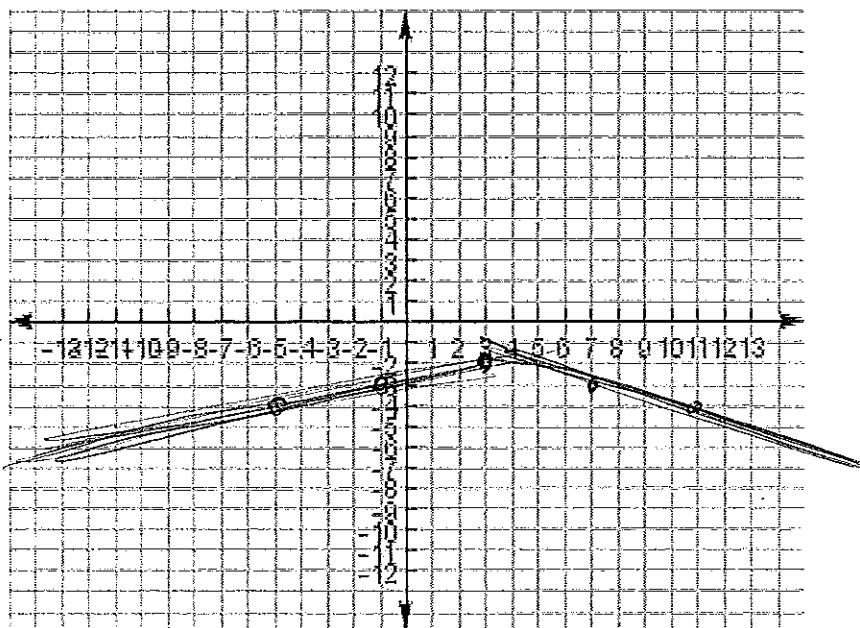
$$(x - 6)^2 + 15$$

$$\begin{aligned} -\frac{12}{2} &= -6 \\ (-6)^2 &= 36 \\ 51 - 36 &= 15. \end{aligned}$$

- 22) State the values of 'a', 'h' and 'k' for the given equation. Then describe how each of these values affects this particular graph. Graph the function.

$$y = -\frac{1}{4}|x - 3| - 2$$

$$\begin{aligned} a &= -\frac{1}{4} && \text{Flip over} \\ && & \text{compress} \\ h &= 3 && \text{Shift right} \\ k &= -2 && \text{Shift down} \end{aligned}$$



- 23) Write an exact equation for a square root function that has a locator point of: (-1, -4) and passes through the point (15, 8).

$$y = a\sqrt{x+1} - 4$$

$$8 = a\sqrt{15+1} - 4$$

$$12 = a\sqrt{16}$$

$$12 = a \cdot 4$$

$$3 = a$$

$$y = 3\sqrt{x+1} - 4$$

- 24) Solve algebraically.

$$8(4x - 5y = 39) \rightarrow 32x - 40y = 312$$

$$y = -\frac{1}{2}x - 4$$

$$5(11x + 8y = -45) \rightarrow 55x + 40y = -225$$

$$3x - 2(-\frac{1}{2}x - 4) = 0$$

$$3x + x + 8 = 0$$

$$4x + 8 = 0$$

$$x = -2$$

$$y = -\frac{1}{2}(-2) - 4$$

$$y = -2 - 4$$

$$y = -6$$

$$4(1) - 5y = 39$$

$$-5y = 35$$

$$y = -7$$

$$x = 1$$

$$(1, -7)$$

- 25) Solve.

$$7|x-1| - 8 = 20$$

$$7|x-1| = 28$$

$$|x-1| = 4$$

$$x-1=4$$

$$\textcircled{x=5}$$

$$x-1=-4$$

$$\textcircled{x=-3}$$

$$\sqrt[4]{x-2} = 6$$

$$x-2 = 6^4$$

$$x-2 = 1296$$

$$\textcircled{x=1298}$$

- 26) Thai Land sells 50 items one busy afternoon. They sell veggie bowls for \$6.00 and desserts for \$7.50. They make a total of \$327. Find how many of each item they sold.

Define your variables. Write a system of equations. Solve it. State your solution.

$$x = \text{veggie bowls}, \quad y = \text{desserts}$$

$$x + y = 50 \rightarrow y = 50 - x$$

$$6x + 7.50y = 327$$

$$6x + 7.50(50 - x) = 327$$

$$6x + 375 - 7.50x = 327$$

$$-1.5x + 375 = 327$$

$$-1.5x = -48$$

$$\textcircled{x=32}$$

$$y = 50 - 32$$

$$y = 18$$