

Operations with Functions Review Packet

**C LEVEL:**

1. Let  $f(x) = x^2(x - 7)(x + 3)^3$  and  $g(x) = x^2(x + 5)(x - 7)$ 
  - a. Find and simplify  $\frac{f(x)}{g(x)}$
  - b. What is the domain and range of  $\frac{f(x)}{g(x)}$  ?
  - c. What is the end behavior (both directions) of  $\frac{f(x)}{g(x)}$  ?
  - d. What are the roots of  $\frac{f(x)}{g(x)}$  ?
  - e. What are the holes of  $\frac{f(x)}{g(x)}$  ?
  - f. What are the asymptotes of  $\frac{f(x)}{g(x)}$  ?
  - g. Sketch a graph of  $\frac{f(x)}{g(x)}$  .
  
2. Let  $p(x) = 3x(x + 10)(x - 4)^2$  and  $q(x) = (x - 4)(x - 5)(x - 6)$ 
  - a. Find and simplify  $\frac{p(x)}{q(x)}$
  - b. What is the domain and range of  $\frac{p(x)}{q(x)}$  ?
  - c. What is the end behavior (both directions) of  $\frac{p(x)}{q(x)}$  ?
  - d. What are the roots of  $\frac{p(x)}{q(x)}$  ?
  - e. What are the holes of  $\frac{p(x)}{q(x)}$  ?
  - f. What are the asymptotes of  $\frac{p(x)}{q(x)}$  ?
  - g. Sketch a graph of  $\frac{p(x)}{q(x)}$  .

3. Mr. Maurer is driving from Portland to Bend (160 miles from PDX) and the trip takes him 3 hours. On his way he drives over Mt. Hood (50 miles from PDX) and the curves in the mountains make him slow down. Once he reaches Warm Springs (100 miles from PDX) the road straightens out and there is no traffic.
- What is his AROC?
  - Does he always drive at that speed?
  - Does he ever drive at exactly that speed?
  - Draw a possible graph of Mr. Maurer's trip to Bend. Please label your axes and any important points.
  - Draw a line that is parallel to the AROC and that lies tangent to your graph.

4. Let  $f(x) = 3x^3 - x^2 - 75x + 25$
- What are the roots of  $f(x)$ ?
  - Sketch a graph of  $f(x)$ . Label roots and y-intercept.
  - Fill in the following table

$x_1$	$x_2$	$\Delta y = y_2 - y_1$	$\frac{\Delta y}{\Delta x}$
0	1		
0	-1		
0	0.1		
0	0.01		
0	0.001		

- What is the instantaneous rate of change at  $x=0$ ?
- Draw the tangent line at  $x=0$

5. Let  $g(x) = x^5 - 50x^3 + 49x$
- What are the roots of  $g(x)$ ?
  - Sketch a graph of  $g(x)$ . Label roots and y-intercept.
  - Fill in the following table

$x_1$	$x_2$	$\Delta y = y_2 - y_1$	$\frac{\Delta y}{\Delta x}$
0	1		
0	-1		
0	0.1		
0	0.01		
0	0.001		

- What is the instantaneous rate of change at  $x=0$ ?
- Draw the tangent line at  $x=0$

### AB LEVEL

1. Let  $p(x) = \frac{x^4 - 22x^2 - 75}{x^4 + 28x^2 + 75}$  and  $q(x) = \frac{x^4 + x^3 - 2x^2 + 4x - 24}{x^4 + 13x^2 + 36}$
- Find and simplify  $p(x) + q(x)$ 
    - What is the domain and range of  $p(x) + q(x)$ ?
    - What is the end behavior (both directions) of  $p(x) + q(x)$ ?
    - What are the roots of  $p(x) + q(x)$ ?
    - What are the holes of  $p(x) + q(x)$ ?
    - What are the asymptotes of  $p(x) + q(x)$ ?
    - Sketch a graph of  $p(x) + q(x)$ .

- b. Find and simplify  $\frac{p(x)}{q(x)}$
- What is the domain and range of  $\frac{p(x)}{q(x)}$  ?
  - What is the end behavior (both directions) of  $\frac{p(x)}{q(x)}$  ?
  - What are the roots of  $\frac{p(x)}{q(x)}$  ?
  - What are the holes of  $\frac{p(x)}{q(x)}$  ?
  - What are the asymptotes of  $\frac{p(x)}{q(x)}$  ?
  - Sketch a graph of  $\frac{p(x)}{q(x)}$  .

2. Let  $p(x) = \frac{x^4 - 5x^3 - 16x^2 + 21x - 9}{x^3 - 9x}$  and  $q(x) = \frac{x^3 + 2x^2 - 56x + 48}{x^2 - 36}$

- a. Find and simplify  $p(x) + q(x)$
- What is the domain and range of  $p(x) + q(x)$ ?
  - What is the end behavior (both directions) of  $p(x) + q(x)$ ?
  - What are the roots of  $p(x) + q(x)$ ?
  - What are the holes of  $p(x) + q(x)$ ?
  - What are the asymptotes of  $p(x) + q(x)$ ?
  - Sketch a graph of  $p(x) + q(x)$ .

- b. Find and simplify  $\frac{p(x)}{q(x)}$
- What is the domain and range of  $\frac{p(x)}{q(x)}$  ?
  - What is the end behavior (both directions) of  $\frac{p(x)}{q(x)}$  ?
  - What are the roots of  $\frac{p(x)}{q(x)}$  ?
  - What are the holes of  $\frac{p(x)}{q(x)}$  ?
  - What are the asymptotes of  $\frac{p(x)}{q(x)}$  ?
  - Sketch a graph of  $\frac{p(x)}{q(x)}$  .

Remember that instantaneous rate of change is defined:  $f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x}$

