## Comparing Compounds

You go to the bank and are offered a choice: How many times a year do you want your money to be compounded? You make tables to compare the different compounding periods. Assume you have $\$ 1000$ and earn $12 \%$ interest.

If you have $12 \%$ interest, that becomes 0.12 as a decimal. That is your ANNUAL interest. To change it to your compound interest, divide by " $n$ " (the number of compounds in a year).

| Compounded Semi-Annually ( $n=2$ )$0.12 \div 2=0.06$ |  |  |  | Compounded Quarterly ( $\mathrm{n}=4$ )$0.12 \div 4=0.03$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Month | Start | Interest | End | Month | Start | Interest | End |
| 1 | 1000 | 0 | 1000 | 1 | 1000 | 0 | 1000 |
| 2 | 1000 | 0 | 1000 | 2 | 1000 | 0 | 1000 |
| 3 | 1000 | 0 | 1000 | 3 | 1000 | 30 | 1030 |
| 4 | 1000 | 0 | 1000 | 4 | 1030 | 0 | 1030 |
| 5 | 1000 | 0 | 1000 | 5 | 1030 | 0 | 1030 |
| 6 | 1000 | 60 | 1060 | 6 | 1030 | 30.90 | 1060.90 |
| 7 | 1060 | 0 | 1060 | 7 | 1060.90 | 0 | 1060.9 |
| 8 | 1060 | 0 | 1060 | 8 | 1060.9 | 0 | 1060.9 |
| 9 | 1060 | 0 | 1060 | 9 | 1060.9 | 31.83 | 1092.73 |
| 10 | 1060 | 0 | 1060 | 10 | 1092.73 | 0 | 1092.73 |
| 11 | 1060 | 0 | 1060 | 11 | 1092.73 | 0 | 1092.73 |
| 12 | 1060 | 63.6 | 1123.60 | 12 | 1092.73 | 32.78 | 1125.51 |

Please notice that there are a lot of months where you DO NOT earn interest. This is what the words "semi-annually" and "quarterly" mean. You do not earn interest every month. For semi-annually, you earn interest every 6 months. That is why the majority of months have the number 0 in the interest column. For quarterly, you earn interest every 3 months.

You can verify the final row in the table by using the compound interest formula: $F=P\left(1+\frac{r}{n}\right)^{n x}$

| $F=1000\left(1+\frac{0.12}{2}\right)^{2 \cdot 1}=1123.6$ | $F=1000\left(1+\frac{0.12}{4}\right)^{4 \cdot 1}=1125.51$ |
| :--- | :--- |

