

Error Analysis – Solving Equations

Directions: Carlos solved the following equations but was having some trouble. In each of the following problems, Carlos made a mistake. See if you can help Carlos fix his mistakes. Examine the problem. When you find the mistake, circle it. Then, in the space provided, explain why it is a mistake, and solve the equation correctly.

Carlos' Work	Explain: What mistake did he make?	Corrected Solution
$3x + 2x - 6 = 24$ $\begin{array}{r} -2x \quad -2x \\ x - 6 = 24 \\ +6 \quad +6 \\ x = 30 \end{array}$	<p>Misused $2x$ twice on left side</p>	$5x - 6 = 24$ $\begin{array}{r} +6 \quad +6 \\ 5x = 30 \\ \hline 5 \quad 5 \\ x = 6 \end{array}$
$-2x + 4 = 12$ $\begin{array}{r} -4 \quad -4 \\ -2x = 8 \\ \hline 2 \quad 2 \\ x = 4 \end{array}$	<p>Divided by positive 2</p>	$-2x = 8$ $\begin{array}{r} \hline -2 \quad -2 \\ x = -4 \end{array}$
$4x - 3 = 17$ $\begin{array}{r} +3 \quad +3 \\ 4x = 20 \\ -4 \quad -4 \\ x = 16 \end{array}$	<p>Misused 4 instead of divided 4.</p>	$\frac{4x = 20}{4 \quad 4}$ $x = 5$
$3(2x - 4) = 8$ $\begin{array}{r} 6x - 4 = 8 \\ +1 \quad +1 \\ 6x = 9 \\ \hline 6 \quad 6 \\ x = 3/2 \end{array}$	<p>Did not distribute 3 to (-4).</p>	$6x - 12 = 8$ $\begin{array}{r} +12 \quad +12 \\ 6x = 20 \\ \hline 6 \quad 6 \\ x = 20/6 \end{array}$

Reflect: Which of these mistakes have you made before? Why do you think you have made those mistakes? How can you avoid these common mistakes?

More on back


Challenge Problems

Identify & fix the error. Each problem is done incorrectly.

$$1) 3 \cdot \left(\frac{x}{3} - 2 = 4 \right) \cdot 3$$

Didn't distribute

$$\frac{x}{3} - 2 = 12$$

+2 +2

$$x = 14$$

Fixed

$$x - 6 = 12$$

+6 +6

$$x = 18$$

$$2) 3 \cdot \left(\frac{x}{3} - \frac{x}{4} = 2 \right) \cdot 3$$

Didn't distribute

$$4 \cdot \left(x - \frac{x}{4} = 6 \right) \cdot 4$$

$$4x - x = 24$$

$$3x = 24$$

$$x = 8$$

$$4 \left(x - \frac{3x}{4} = 6 \right) \cdot 4$$

$$4x - 3x = 24$$

$$x = 24$$

$$3) x^2 + 1 = 26$$

$$x^2 = 25$$
$$x = 12.5$$

Didn't square root

$$x^2 = 25$$

$$x = 5 \text{ or } x = -5$$