

## Factoring Quadratic Expressions

Factor each completely.

1)  $x^2 - 7x - 18$

$$\begin{array}{r|l} x & x^2 - 7x \\ \hline 2 & -18 \end{array} = (x-9)(x+2)$$

2)  $p^2 - 5p - 14$

$$\begin{array}{r|l} p & p^2 - 5p \\ +2 & -14 \end{array} = (p-7)(p+2)$$

3)  $m^2 - 9m + 8$

$$\begin{array}{r|l} m & m^2 - 9m \\ -8 & 8 \end{array} = (m-1)(m-8)$$

4)  $x^2 - 16x + 63$

$$\begin{array}{r|l} x & x^2 - 16x \\ -7 & 63 \end{array} = (x-9)(x-7)$$

5)  $7x^2 - 31x - 20$

$$\begin{array}{r|l} 7x+4 & 7x^2 - 31x \\ -5 & -20 \end{array} = (7x+4)(x-5)$$

6)  $7k^2 + 9k$

$$k(7k+9)$$

7)  $7x^2 - 45x - 28$

$$\begin{array}{r|l} 7x+4 & 7x^2 - 45x \\ 7 & -28 \end{array} = (7x+4)(x-7)$$

8)  $2b^2 + 17b + 21$

$$\begin{array}{r|l} 2b+3 & 2b^2 + 17b \\ 7 & 21 \end{array} = (2b+3)(b+7)$$

9)  $5p^2 - p - 18$

$$\begin{array}{r|l} 5p+9 & 5p^2 - p \\ -2 & -18 \end{array} = (5p+9)(p-2)$$

$$10) 28n^4 + 16n^3 - 80n^2 = 4(7n^4 + 4n^3 - 20n^2)$$

$$= 4n^2(7n^2 + 4n - 20)$$

$$= 4n^2(n+2)(7n-10)$$

$$\begin{array}{r|l} n & 7n^2 + 4n \\ +2 & -20 \end{array}$$

$$11) 3b^3 - 5b^2 + 2b = b(3b^2 - 5b + 2)$$

$b$	$3b^2$	$-2b$
$-1$	$-3b$	$2$

$$= b(b-1)(3b-2)$$

$$12) 7x^2 - 32x - 60$$

$x$	$7x^2$	$10x$
$-6$	$-42x$	$-60$

$$= (7x+10)(x-6)$$

$$13) 30n^2b - 87nb + 30b = 3b(10n^2 - 29n + 10)$$

$2n$	$10n^2$	$-4n$
$-5$	$-25n$	$10$

$$= 3b(2n-5)(5n-2)$$

$$14) 9r^2 - 5r - 10$$

$3r$	$9r^2$	$5$
$2$	$-10$	$-5r$

$45 \div 9 = 5$   
 $3 \cdot 3 = 5 \cdot 2$   
 $15 = 6$   
 $30 = 3$

~~Factorable~~

$$15) 9p^2r + 73pr + 70r = r(9p^2 + 73p + 70)$$

$p$	$9p^2$	$10p$
$7$	$63p$	$70$

$$= r(p+7)(9p+10)$$

$9x^2$	$56$
$-56$	$7$

$8 \cdot 7 = 56$

~~Factorable~~

$$17) 4x^3 + 43x^2 + 30x = x(4x^2 + 43x + 30)$$

$x$	$4x^2$	$3x$
$10$	$40x$	$30$

$$= x(4x+3)(x+10)$$

$$18) 10m^2 + 89m - 9$$

$m$	$10m^2$	$-1m$
$9$	$90m$	$-9$

$$= (10m-1)(m+9)$$

**Critical thinking questions:**

19) For what values of  $b$  is the expression factorable?

$$x^2 + bx + 12$$

$$12 = 1 \cdot 12$$

$$2 \cdot 6$$

$$3 \cdot 4$$

$$\text{So } b = \pm 13, \pm 8, \pm 7$$

20) Name four values of  $b$  which make the expression factorable:

$$x^2 - 3x + b$$

Infinite possibilities.

$$b = -24 \quad (-4 + 1 = -3)$$

$$b = -10 \quad (-5 + 2 = -3)$$

$$b = 0 \quad (-3 + 0 = -3)$$

$$b = -18 \quad (-6 + 3 = -3)$$