

I can find the INVERSE of a function algebraically.

The first step to finding the inverse of

$h(x) = \sqrt{2x+1} + 5$ is to switch the X

and the y to form the equation

$x = \sqrt{2y+1} + 5$

Then solve this equation for y by

Reversing Operations.

$x = \sqrt{2y+1} + 5$
 $-5 \qquad -5$

$x - 5 = \sqrt{2y+1}$

$(x-5)^2 = 2y+1$

$\frac{(x-5)^2 - 1}{2} = y^{-1} = h^{-1}(x)$

I can find the INVERSE from a given table.

The table representing the inverse $f^{-1}(x)$ can be

created by switching x & y

x	f(x)
-8	-2
-1	-1
0	0
1	1
8	2

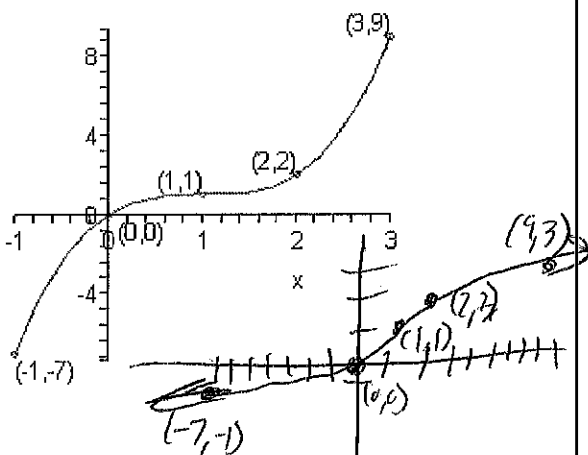
x	$f^{-1}(x)$
-2	-8
-1	-1
0	0
1	1
2	8

I can graph the INVERSE from a given graph.

To draw the INVERSE, I locate points on the

original graph and switch the x and the y and

graph these new points.

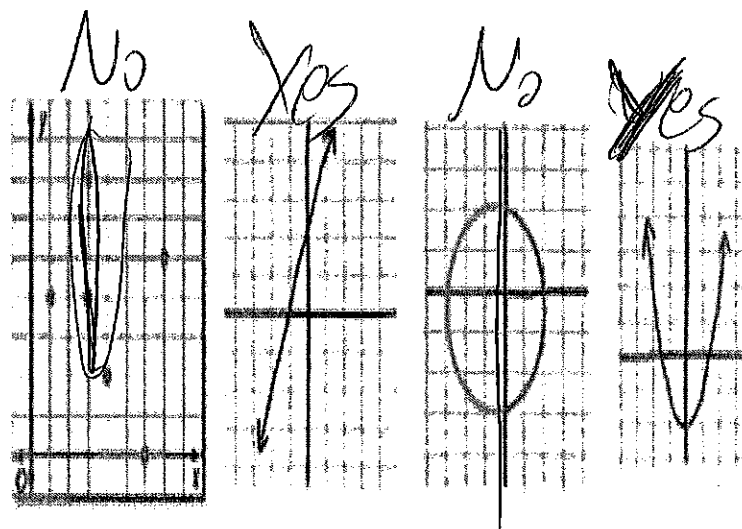


I can use a graph to determine whether or not a RELATION is a FUNCTION.

The vertical Line Test shows that a

RELATION is a function if any vertical line

hits the graph in AT MOST one point.



I can use a table to determine whether or not a RELATION is a FUNCTION.

If a table has repeated X values that have different y values then the table

is not a function

If each X value in a table has only one

y

value then the table

is a

function

x	y
3	3
4	5
5	7
5	9
6	11

No

x	y
5	31
6	28
7	25
8	22
9	19

Yes

x	y
2	3
3	3
4	3
5	3
6	3

Yes

x	y
7	10
8	20
9	30
9	40
10	50

No

I can use COMPOSITE FUNCTIONS to determine whether or not two functions are INVERSES.

$$f(x) = 2\sqrt{x-1} + 2 \text{ and } g(x) = \left(\frac{x-2}{2}\right)^2 + 1$$

The COMPOSITE FUNCTION $f(g(x))$ means you

replace the x in $f(x)$ with $g(x)$

$$2\sqrt{\left(\frac{x-2}{2}\right)^2 - 1} + 2$$

$$2\sqrt{\left(\frac{x-2}{2}\right)^2} + 2$$

$$2\left(\frac{x-2}{2}\right) + 2 = x - 2 + 2 = x$$

If two functions are INVERSES then $f(g(x))$

simplifies to x . This makes sense because

if two functions are INVERSES, combining the two

functions should cancel out

Function Practice: Let $f(x) = (x-3)^3 + 5$ and $g(x) = \sqrt[3]{x-5} + 3$

Find the following:

1. $f(3) = (3-3)^3 + 5 = 5$

2. $g(5) = \sqrt[3]{5-5} + 3 = \sqrt[3]{0} + 3 = 3$

3. $g(f(0)) = g((0-3)^3 + 5) = g(-27+5) = g(-22) = \sqrt[3]{-22-5} + 3 = \sqrt[3]{-27} + 3 = -3 + 3 = 0$

4. $f(g(4)) = 4$

Solve the following:

5. $f(x) = 5$
 $(x-3)^3 + 5 = 5$
 $(x-3)^3 = 0$
 $x-3 = 0$
 $x = 3$

6. $g(x) = 3$
 $\sqrt[3]{x-5} + 3 = 3$
 $\sqrt[3]{x-5} = 0$
 $x-5 = 0$
 $x = 5$

7. $f(x) = 4$
 $(x-3)^3 + 5 = 4$
 $(x-3)^3 = -1$
 $x-3 = -1$
 $x = 2$

8. $g(x) = 0$
 $\sqrt[3]{x-5} + 3 = 0$
 $\sqrt[3]{x-5} = -3$
 $x-5 = -27$
 $x = -22$

Simplify the following:

9. $f(g(x))$
 $(\sqrt[3]{x-5} + 3 - 3)^3 + 5$
 $(\sqrt[3]{x-5})^3 + 5$
 $x-5 + 5 = x$

10. $g(f(x))$
 $\sqrt[3]{(x-3)^3 + 5 - 5} + 3$
 $\sqrt[3]{(x-3)^3} + 3$
 $x-3 + 3 = x$