

Worksheet AA4-4: Unit 4 Parabola Practice

1) Write the equation of a parabola with the following features.

Open up/down	Stretch factor	Vertex	Equation
a) Up	1	(2, -5)	$y = 1(x-2)^2 - 5$
b) Up	0.5	(0, 4)	$y = 0.5(x)^2 + 4$
c) Down	2	(-10, -7)	$y = 2(x+10)^2 - 7$
d) Down	5	(6, 0)	$y = 5(x-6)^2$
e) Up	0.75	(4, 8)	$y = 0.75(x-4)^2 + 8$

2) Analyze the features of the following parabolas by completing the table for each equation.

Equation	Open up/down	Stretch factor	Relative width (narrow/wide/"normal")	Location of vertex
a) $f(x) = 2(x+4)^2 - 6$	Up	2	Narrow	(-4, -6)
b) $f(x) = 0.5x^2 + 5$	Up	0.5	Wide	(0, 5)
c) $f(x) = -4(x-2)^2 - 10$	Down	-4	Narrow	(2, -10)
d) $f(x) = (x-1)^2$	Up	1	Normal	(1, 0)
e) $f(x) = -0.75(x+8)^2 + 3$	Down	-0.75	Wide	(-8, 3)

3) Find the equation of the parabola with the given vertex, passing thru the given point.

a) Vertex (-2, 3) point (0, 8)

$$y = a(x+2)^2 + 3$$

$$8 = a(0+2)^2 + 3$$

$$8 = a(2)^2 + 3$$

$$-3 = -3$$

$$5 = 4a$$

$$a = \frac{5}{4}$$

$$y = \frac{5}{4}(x+2)^2 + 3$$

b) Vertex (4, -6) point (2, -7)

$$y = a(x-4)^2 - 6$$

$$-7 = a(2-4)^2 - 6$$

$$-7 = a(-2)^2 - 6$$

$$-7 = 4a - 6$$

$$-1 = 4a$$

$$-\frac{1}{4} = a$$

$$y = -\frac{1}{4}(x-4)^2 - 6$$

c) Vertex (10, 40) point (4, 0)

$$y = a(x-10)^2 + 40$$

$$0 = a(4-10)^2 + 40$$

$$0 = a(-6)^2 + 40$$

$$0 = 36a + 40$$

$$-40 = 36a$$

$$-\frac{40}{36} = a = -\frac{10}{9}$$

$$y = -\frac{10}{9}(x-10)^2 + 40$$

d) Vertex (0, 50) point (75, 0)

$$y = a(x)^2 + 50$$

$$0 = a(75)^2 + 50$$

$$0 = a(5625) + 50$$

$$-50 = a \cdot 5625$$

$$-\frac{50}{5625} = a = -\frac{2}{225}$$

$$y = -\frac{2}{225}x^2 + 50$$

4) Find the vertex of each parabola and write the equation in vertex form.

a) $y = x^2 + 10x + 24$

$y = (x + 5)^2 - 1$ $V: (-5, -1)$

x^2	$5x$	24
$5x$	25	-25

b) $y = x^2 - 4x - 12$

$y = (x - 2)^2 - 16$ $V: (2, -16)$

x^2	$-2x$	-12
$-2x$	4	-4

c) $y = 2x^2 - 9x - 1$

$y = 2(x^2 - \frac{9}{2}x) - 1$

$y = 2((x - \frac{9}{4})^2 - \frac{81}{16}) - 1 = 2(x - \frac{9}{4})^2 - \frac{81}{8} - 1$

x^2	$-\frac{9}{4}x$	$-\frac{81}{16}$
$-\frac{9}{4}x$	$\frac{81}{16}$	

$y = 2(x - \frac{9}{4})^2 - \frac{89}{8}$
 $V: (\frac{9}{4}, -\frac{89}{8})$

d) $y = (x + 5)(x - 3)$

$x^2 + 5x - 3x - 15$

$x^2 + 2x - 15$

$(x + 1)^2 - 16$

x^2	$1x$	-15
$1x$	1	-1

$V: (-1, -16)$

e) $y = x^2 + 5x - 14$

x^2	$2.5x$	-14
$2.5x$	6.25	

$2.5x$	6.25	-6.25
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$(x + 2.5)^2 - 20.25$

$V: (-2.5, -20.25)$

f) $y = 2(x + 3)(x - 9)$

$y = 2(x^2 + 3x - 9x - 27)$

$y = 2(x^2 - 6x - 27)$

$y = 2((x - 3)^2 - 36)$

x^2	$-3x$	-27
$-3x$	9	-9

$y = 2(x - 3)^2 - 72$

$y = 2(x - 3)^2 - 72$

$V: (3, -72)$