

1. After factoring, sketch the graph of the equation  $y = -x^3 + 2x^2 - x$ . Remember to look for common terms.

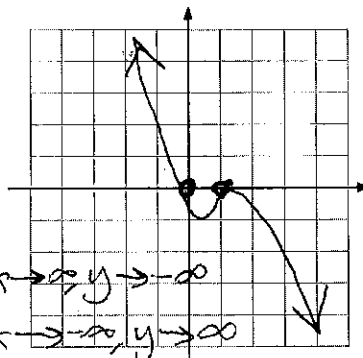
$$y = -x(x^2 - 2x + 1)$$

$$-x(x-1)(x-1)$$

$$-x(x-1)^2$$

Roots = 0, 1, 1  
Multiplicity: 1, 2

E.B. As  $x \rightarrow \infty, y \rightarrow -\infty$   
As  $x \rightarrow -\infty, y \rightarrow \infty$

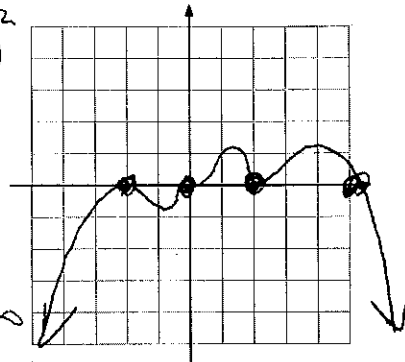


2. Sketch the graph of the equation with a double root at -2, a single root at 5, a triple root at 0 and a double root at 2. Assume the leading coefficient is negative. Write the equation of the function that describes the graph.

Equation:  $-5(x+2)^2(x-5)x^3(x-2)^2$

Degree = 8  
L.C. = -5

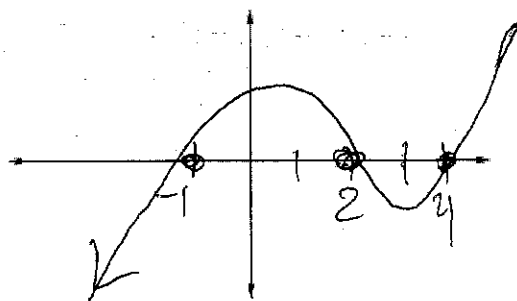
E.B. As  $x \rightarrow \infty, f(x) \rightarrow -\infty$   
As  $x \rightarrow -\infty, f(x) \rightarrow -\infty$



Sketch the graph of each function.

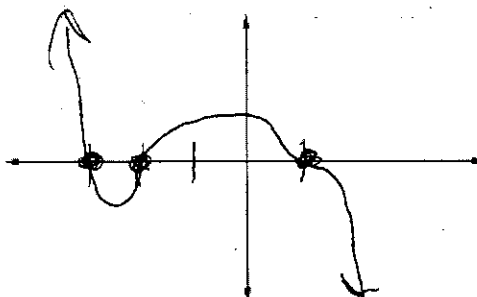
7.  $f(x) = (x+1)(x-2)(x-4)$

Degree = 3  
L.C. = 1



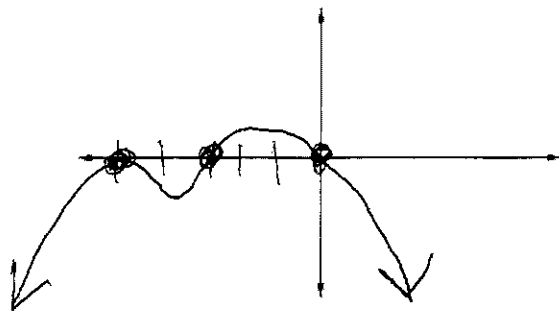
8.  $f(x) = -(x+3)(x+2)(x-1)^3$

Degree = 5  
L.C. = -1



9.  $f(x) = -x(x+5)^2(x+3)$

Degree = 4  
 L.C = -1

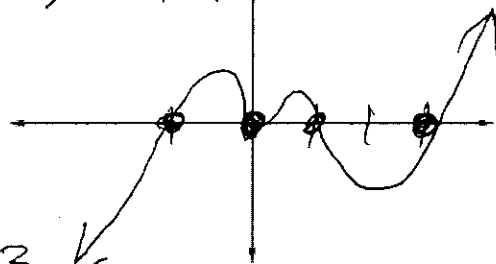


10.  $f(x) = x^5 - 3x^4 - x^3 + 3x^2 = x^2(x^3 - 3x^2 - x + 3) = x^2(x+1)(x-1)(x-3)$

Given that  $f(-1) = f(1) = 0$

$f(-1) = 0 \rightarrow (x+1)$   
 $f(1) = 0 \rightarrow (x-1)$

Degree = 5  
 L.C = 1



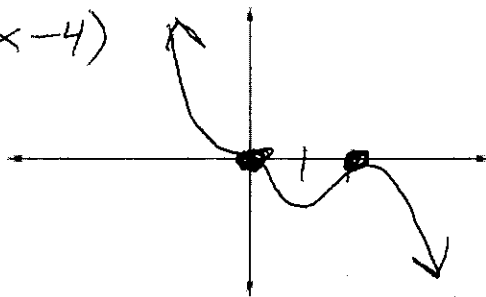
	$x^2 - 2x - 3$		
$x$	$x^3$	$-2x^2$	$-3x$
$-1$	$-x^2$	$2x$	$3$

$x^2 - 2x - 3$   
 $(x-3)(x+1)$

11.  $f(x) = -x^5 + 4x^4 - 4x^3 = -x^3(x^2 + 4x - 4)$

Given that  $f(2) = 0$

$= -x^3(x-2)^2$



12.  $f(x) = x^2(x-1)^2(2+x)$

