

**1. Zero Exponents**

- a. Since 2000, college tuition has been growing substantially. For example, the cost of tuition at the University of Oregon since 2000 can be represented by the function  $t(x) = 3800 \cdot 1.26^{\frac{x}{4}}$ , where  $x =$  years since 2000 and  $y =$  tuition for Oregon residents.
- What does the  $1.26^{\frac{x}{4}}$  in the equation tell you about the cost of tuition? Be specific and complete.
  - Evaluate  $t(0)$ . What does  $t(0)$  mean about the cost of tuition?
- b. For any exponential equation,  $f(x) = a \cdot b^x$ , explain why  $f(0) = a$ .
- c. Given part (b), it must be true that  $a = a \cdot b^0$  for any exponential equation. Why does this mean that  $b^0 = 1$  for any value  $b$ ? Explain thoroughly.

**2. Negative Exponents**

- a. I started college in 1984. Use the equation from 1a above to determine tuition in 1984 (recall that  $x =$  years since 2000) at the U of O.
- b. What exponent did you use in 2a to go back to 1984? What effect did a negative exponent have on the year 2000 tuition?
- c. Without using a calculator, predict what the value of  $10 \cdot 2^{-1} =$  \_\_\_\_\_. Why do you think it will be that value?

- d. Recall that exponents are human inventions to provide a shortcut for repeated multiplication. For example,  $10 \cdot 2^3 = 10 \cdot 2 \cdot 2 \cdot 2$  and  $10 \cdot 2^2 = 10 \cdot 2 \cdot 2$  and  $10 \cdot 2^1 = 10 \cdot 2$  and  $10 \cdot 2^0 = 10$ . Given this pattern, what do you think  $10 \cdot 2^{-1} = \underline{\hspace{2cm}}$ ? What about  $10 \cdot 2^{-2} = \underline{\hspace{2cm}}$ ?

- e. Use this to explain why  $y = 2^{-x}$  is equivalent to  $y = (\frac{1}{2})^x$ .

### 3. Fraction Exponents and Roots

- a. Use the equation from question 1 to determine the U of O tuition in 2001. In other words, evaluate  $t(1) = 3800 \cdot 1.26^{\frac{1}{4}}$ .

- b. In question 1ai, you should have made a statement equivalent to “ $1.26^{\frac{1}{4}}$  means that tuition grew by 26% every 4 years.” How could you use the answer to 3a to determine the one-year growth rate of tuition?

- c. What does it mean to raise a number to a fractional exponent. Consider the examples below:

$$9^{\frac{1}{2}} = (3 \cdot 3)^{\frac{1}{2}} = 3 \qquad 16^{\frac{1}{4}} = (2 \cdot 2 \cdot 2 \cdot 2)^{\frac{1}{4}} = 2 \qquad 125^{\frac{1}{3}} = (5 \cdot 5 \cdot 5)^{\frac{1}{3}} = 5$$

So what does  $100^{\frac{1}{2}} = \underline{\hspace{2cm}}$ ?  $8^{\frac{1}{3}} = \underline{\hspace{2cm}}$ ?

- d. A fractional exponent is equivalent to taking a root. For example,  $a^{\frac{1}{2}} = \sqrt{a}$  and  $b^{\frac{1}{3}} = \sqrt[3]{b}$ . Given part c above, explain why this makes sense.