

Day 29: Using Function Notation to Solve Problems

Last class we learned about function notation as a way to communicate which equation or line we are talking about. Remember that we named Ian Maurer's equation $I(x)$ (pronounced "I of x"), Ellen Maiden's equations $E(x)$ (pronounced "E of x") and Chelsea Muhs' equation as $C(x)$ (pronounced C of x).

We can use function notation to solve problems. For example, if you have a function $f(x) = 2x + 3$, and you want to know what $f(x)$ is equal to when x equals 5, you write it like this-- Find $f(5)$:

$$f(5) = 2(5) + 3$$

$$10 + 3 = 13$$

If you know a certain **y-value** and want to find the corresponding **x-value**, you can also use function notation. Let's say you want to know what x is when $y = 45$, you write it like this -- Solve $f(x) = 45$:

$$2x + 3 = 45$$

$$\begin{array}{r} -3 \\ -3 \end{array}$$

$$\frac{2x}{2} = \frac{42}{2} \rightarrow x = 21$$

Let's apply these skills to solve problems about "The Big Race":

During Heat 2, Chelsea Muhs' run could be modeled with the equation $C(x) = 5x - 10$, because she could run 5 yards per second, and she started 10 yards behind the starting line. Remember, x represents the time in seconds, and $C(x)$, or y , represents the distance in yards.

1. What was her distance after 20 seconds of running?

$$C(20) = 5(20) - 10$$

$$100 - 10$$

$$C(20) = 90$$

3. Find
- $C(40)$
- .

$$C(40) = 5(40) - 10$$

$$200 - 10$$

$$C(40) = 190$$

5. How many seconds will it take her to run 95 meters?

$$5x - 10 = 95$$

$$\begin{array}{r} +10 \\ +10 \end{array}$$

$$\frac{5x}{5} = \frac{105}{5} \rightarrow x = 21$$

2. Find
- $C(23)$
- .

$$C(23) = 5(23) - 10$$

$$115 - 10$$

$$C(23) = 105$$

4. What does the result mean of #3?

After 40 seconds,
Ms. Muhs is 190
yards into the race.

6. Solve
- $C(x) = 25$

$$5x - 10 = 25$$

$$\begin{array}{r} +10 \\ +10 \end{array}$$

$$\frac{5x}{5} = \frac{35}{5} \rightarrow x = 7$$

7. What does the result mean of #6?

After 7 seconds, the runner is 25 yards.

Use these two functions for the following problems: $f(x) = 12x + 1$ and $g(x) = -4x + 8$

8. Find $f(4)$.

$$f(4) = 12(4) + 1$$
$$48 + 1$$

$$f(4) = 49$$

9. Find $f(-3)$.

$$f(-3) = 12(-3) + 1$$
$$-36 + 1$$

$$f(-3) = -35$$

10. Find $g(4)$.

$$g(4) = -4(4) + 8$$
$$-16 + 8$$

$$g(4) = -8$$

11. Find $g(-3)$.

$$g(-3) = -4(-3) + 8$$
$$12 + 8$$

$$g(-3) = 20$$

12. Solve $f(x) = 25$

$$12x + 1 = 25$$
$$-1 \quad -1$$

$$12x = 24$$
$$\frac{12x}{12} = \frac{24}{12}$$

$$x = 2$$

13. Solve $g(x) = -36$

$$-4x + 8 = -36$$
$$-8 \quad +8$$

$$-4x = -44$$
$$\frac{-4x}{-4} = \frac{-44}{-4}$$

$$x = 11$$

14. Solve $g(x) = 10$

$$-4x + 8 = 10$$
$$-8 \quad -8$$

$$-4x = 2$$
$$\frac{-4x}{-4} = \frac{2}{-4}$$

$$x = -\frac{1}{2}$$

15. Solve $f(x) = 10$

$$12x + 1 = 10$$
$$-1 \quad -1$$

$$12x = 9$$
$$\frac{12x}{12} = \frac{9}{12}$$

$$x = \frac{3}{4}$$